

DEPARTMENT OF CIVIL ENGINEERING
COURSE SYLLABUS

Course Details					
Code				Academic Year	Semester
MAT106				1	Spring
Title	T	A	L	ECTS	
Linear Algebra	2	2	1	6	
Language	German				
Level	Undergraduate	X	Graduate		Postgraduate
Department / Program	Civil Engineering				
Forms of Teaching and Learning	Formal				
Course Type	Compulsory	X	Elective		
Objectives	This course covers matrix theory and linear algebra. Emphasis is given to topics that will be useful in other disciplines, including systems of equations, vector spaces, determinants and eigenvalues. After successfully completing this course, you will have a good understanding of the following topics and their applications: systems of linear equations, row reduction and echelon forms, matrix operations, linear dependence and independence, vector spaces and subspaces, orthogonal bases and orthogonal projections, Gram-Schmidt process, linear models and least-squares problems, determinants and their properties, Cramer's Rule, eigenvalues and eigenvectors, diagonalization of a matrix, Markov matrices.				
Content	<ul style="list-style-type: none"> - Vectors, Matrices - Linear Equations, Gauss-Jordan - Vector Spaces, the four fundamental subspaces, Nullspace, Column Space - Dimension, Basis, Span - Orthogonal vectors and subspaces, projections - Orthogonal matrices and Gram-Schmidt - Determinants, Cramer's rule - Eigenvalues, Eigenvectors, Diagonalization and Powers of A - Differential Equations, $\exp(A)$ - Markov Matrices 				
Prerequisites	None				
Coordinator					
Lecturer(s)					
Assistant(s)					
Work Placement	None				
Recommended or Required Reading					
Books / Lecture Notes	<ul style="list-style-type: none"> - Strang, Gilbert. <i>Lineare Algebra</i>. Springer-Verlag Berlin Heidelberg GmbH, 2003. - Teschl, Gerald; Teschl, Susanne. <i>Mathematik für Informatiker, Band 1: Diskrete</i> - <i>Mathematik und Lineare Algebra</i>. Springer-Verlag Berlin Heidelberg 2006, 2007. 				
Other Sources	<ul style="list-style-type: none"> - Göllmann, Laurenz et.al. <i>Mathematik für Ingenieure: Verstehen, Rechnen, Anwenden</i>. Springer Vieweg, 2017. 				

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	- Gilbert Strang. <i>18.06SC Linear Algebra</i> . Fall 2011. Massachusetts Institute of Technology: MIT OpenCourseWare, https://ocw.mit.edu . License: Creative Commons BY-NC-SA . Accessed 2020-03-14.
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Additional Course Material

Documents	https://www.geogebra.org/u/canan.yildiz
Assignments	-
Exams	-

Course Composition

Mathematics und Basic Sciences	100	%
Engineering		%
Engineering Design		%
Social Sciences		%
Educational Sciences		%
Natural Sciences		%
Health Sciences		%
Expert Knowledge		%

Assessment

Activity	Count	Percentage (%)
Midterm Exam	1	40
Quiz		
Assignments	1	10
Attendance		
Recitations		
Projects		
Final Exam	1	50
Total		100

ECTS Points and Work Load

Activity	Count	Duration	Work Load (Hours)
Lectures	14	2	28
Self-Study	1	62	6 2
Assignments	10	3	30
Presentation / Seminar Preparation			
Midterm Exam	1	3	3
Recitations	14	2	2 8
Laboratory	14	1	14
Projects			

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Final Exam	1	3	3
Total Work Load			168
ECTS Points (Total Work Load / 28)			6

Learning Outcomes

1	Solving $Ax = b$ for square systems by elimination (pivots, multipliers, back substitution, invertibility of A , factorization into $A = LU$)
2	Complete solution to $Ax = b$ (column space containing b , rank of A , null space of A and special solutions to $Ax = 0$ from row reduced R)
3	Basis and dimension (bases for the four fundamental subspaces)
4	Least squares solutions (closest line by understanding projections)
5	Orthogonalization by Gram-Schmidt (factorization into $A = QR$)
6	Properties of determinants (leading to the cofactor formula and the sum over all $n!$ permutations, applications to $\text{inv}(A)$ and volume)
7	Eigenvalues and eigenvectors (diagonalizing A , computing powers A^k and matrix exponentials to solve difference and differential equations)
8	Linear transformations and change of basis (connected to the Singular Value Decomposition - orthonormal bases that diagonalize A)
9	Linear algebra applications (graphs and networks, Markov matrices, linear programming)

Weekly Content

1	Introduction, vectors
2	Span, bases, linear independence, vector spaces, subspaces
3	Linear transformations and matrices
4	Matrix multiplication and composition, systems of equations and their geometry
5	Elimination with matrices, Gauss-Jordan algorithm
6	Null space ($Ax = 0$), column space, row space and their dimensions
7	Dot product, orthogonal vectors, projections
8	Orthogonal projections, Least Squares
9	Midterm Exams
10	Orthonormal vectors and Gram-Schmidt
11	Properties and applications of determinants
12	Eigenvectors and eigenvalues
13	Diagonalization
14	Markov matrices
15	Summary, exercise

Contribution of Learning Outcomes to Program Objectives (1-5)

	P1	P2	P3	P4	P5	P6	P7
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1	5	5	4			3	1
2	5	5	4			3	1
3	5	5	4			3	1
4	5	5	4			3	1
5	5	5	3			3	1
6	5	5	3			3	1
7	5	5	3			3	1
8	5	5	3			3	1
9	5	5	3			3	1
Contribution Level	1: Low 2: Low-intermediate 3: Intermediate 4: High 5: Very High						
Compiled by:							
Date of Compilation:	14.03.2020						