

Course Details							
Code				Acad	Academic Year		Semester
MAT108				1	1		Spring
Title				Т	Α	L	ECTS
Calculus 2			3	2	0	6	
Language	German						
Level	Undergraduate	х	Graduate		Postgraduate		aduate
Department / Program	Mechatronic Eng	gineering					
Forms of Teaching and Learning	Face-to-Face, Group Study, Individual Study.						
Course Type	Compulsory		x		Elective		
Objectives	<ul> <li>In this course students should</li> <li>master differential and integral calculus for functions of several variables as a prerequisite for dealing with mathematical models of engineering,</li> <li>develop an understanding of and the ability to work with functions in multidimensional space, master vector calculations in multidimensional space,</li> <li>have a sound knowledge of the scientific and mathematical concepts, principles and methods of the natural and engineering sciences,</li> <li>master basic terms and techniques and apply them to various (e.g. physical) problems,</li> <li>use digital technologies effectively to solve problems.</li> </ul> Knowledge & Understanding: 70% Analysis & methodology: 30%						
Content	<ul> <li>Parameter display</li> <li>Polar coordinates</li> <li>Vectors, lines and planes in space</li> <li>Vector functions and movement in space</li> <li>Functions of several variables</li> <li>Partial derivatives, directional derivative, gradient</li> <li>Applications of multivariable differential calculus</li> <li>Multiple integrals</li> <li>Multiple integrals in polar coordinates</li> <li>Applications of integrals with multiple variables</li> <li>Vector fields, integrals along curves, surface integrals</li> </ul>						
Prerequisites	Recommended: Ca	alculus 1					
Coordinator	PD.Dr.habil. Emre	IŞIK					
Lecturer(s)	PD.Dr.habil. Emre	IŞIK					
Assistant(s)	MSc. Ozan Subaşı MSc. Arda Çetiner BSc. Mustafa Korkut Özarslan						
Work Placement	None						
Recommended or Required R	eading						



	COOKSE 3				
Books / Lecture Notes	<ul> <li>George B. Thomas, Analysis 2, Pearson Deutschland, Hallbergmoos 2013.</li> <li>Papula Lothar, Mathematik für Ingenieure und Naturwissenschaftler, Band 2+3, Wiesbaden 2011.</li> <li>Şanal Ziya, Mathematik für Ingenieure, Vieweg+Teubner, Wiesbaden 2009.</li> </ul>				
Other Sources	<ul> <li>Jana Ziya, Mathematik für ingenieure, Vieweg+Fedbrief, Wiesbaden 2009.</li> <li>David Jerison, and Arthur Mattuck. MIT OpenCourseWare, <u>18.02 Multivariable Calculus</u>. URL: https://ocw.mit.edu/courses/mathematics/18-02-multivariable-calculus-spring- 2006/ [16-03-2020]</li> </ul>				
Additional Course Material					
Documents	https://www.geogebra.org/u/c OneNote Notizbuch MAT108	anan.yildiz			
Assignments	-				
Exams	-				
Course Composition					
Mathematics und Basic Sciences	10	%			
Engineering			%		
Engineering Design			%		
Social Sciences			%		
Educational Sciences			%		
Natural Sciences			%		
Health Sciences			%		
Expert Knowledge			%		
Assessment					
Activity	Cou	nt	Percentage (%)		
Midterm Exam	1	30			
Quiz	1	20			
Assignments					
Attendance					
Recitations					
Projects					
Final Exam	1	1			
		Total	100		
ECTS Points and Work Load					
Activity	Count	Duration	Work Load (Hours)		
Lectures	14	3	42		
Self-Study	1	62	62		
Assignments	10	3	30		
Presentation / Seminar Preparation					
Midterm Exam	1	3	3		



		COURSE 3					
Recitations		14	2	28			
Laboratory							
Projects							
Final Exam		1	3	3			
Total Work Load 168							
	ECTS Points (Total Work Load / 28)6						
Learning Outco	omes						
1	Parametrizatio	on of curves, calculus with param	etrized curves				
2		vatives, tangents, surfaces and ar					
3	Vectors, angles between vectors, vector projections in space; Cross product of two vectors in space, determinant, the mixed product (spat product)						
4	Vectors and parametrized lines and planes in space, angle between planes						
5	Vector valued functions; Curves, derivatives and movement in space, integrals of vector functions						
6	Functions of several variables, graphs, contour lines						
7	Second and higher order partial derivatives, mixed derivatives, differentiability						
8	Chain rule for functions of two and three variables, implicit differentiation						
9	Directional derivations, calculation of gradients, gradients and tangents on contour lines						
10	Tangential planes, linearization, error estimation, differentials, the total differential						
11	Extreme values and saddle points, Hesse matrix, Lagrange multipliers						
12	Double integrals over restricted areas, volumes, determination and exchange of the integration limits, double integrals in polar form, masses and center of mass						
13	Line integrals, vector fields, gradient fields, work as an integral, flow integrals and circulation						
14	Path independence, conservative fields, gradient fields and potential functions; Surface integrals, flow of a vector field through an oriented surface						
Weekly Conter	nt						
1	Overview, introduction of multivariable functions, parametrization						
2	Polar coordinates (points, intervals, point sets, curves, areas), calculation of areas in polar coordinates						
3	Lines and planes in space, curves in space, tangents, vector functions, movement along a curve						
4	Functions of several variables, partial derivatives, meaning of the partial derivative, slope in one point						
5	Generalized ch	nain rule, directional derivative, g	radient				
6	Tangential pla	nes and differentials					
7	Extreme values and saddle points, Lagrange multipliers						
8	Double integrals, determination of the integration limits						
9	Midterm exams						

10 Double integrals, swapping the integral limits, double integrals with polar coordinates11Triple integrals, mass, center of mass12Vector fields line integrals13Line integrals of vector fields, work along curves, flow integrals and circulation14Flow through a flat curve, conservative fields, potential functions14Flow through a flat curve, conservative fields, determination of potentials, divergence and rotationContribution of P1P1P2P3P4P5P6P7P8P9P10P1555344535553445455555344555553445555534454555534555553445455553454555534545555345455553555365557777777 <t< th=""><th></th></t<>					
12       Vector fields line integrals         13       Line integrals of vector fields, work along curves, flow integrals and circulation         14       Flow through a flat curve, conservative fields, gotential function         15       Line integrals in conservative fields, determination of potentials, divergence and circulation         15       Line integrals in conservative fields, determination of potentials, divergence and circulation         Contribution of P1       P2       P3       P4       P5       P6       P7       P8       P9       P10       P11         1       5       5       5       3       4       4       5       4       5         2       P1       P2       P3       P4       P5       P6       P7       P8       P9       P10       P11         1       5       5       5       3       4       4       5       4       5         2       55       55       5       3       4       4       5       4       5         3       5       5       5       3       4       4       5       4       5         4       5       5       5       3       4       4       5       4       5 </th <th></th>					
Image: Second					
14Flow through a flat curve, conservative fields, potential functions15Line integrals in conservative fields, determination of potentials, divergence and rotationContribution of Learning Outcomes to Program Objectives (1-5)1P2P3P4P5P6P7P8P9P10P111555534454525555553445453555344545355534454545553445454555344545555344545455534454555534454545553445455553445456555344545655534454565553445457899 <th></th>					
Ine integrals in conservative fields, determination of potentials, divergence and rotationContribution of P2P3P4P5P6P7P8P9P10P111555534454525555553445453555344545355534454535555344545455534454545553445455553445454555344545555344545455534454555534454555534454565534454565534454565534454 </th <th></th>					
Ine integrals in conservative fields, determination of potentials, divergence and rotation         Contribution of Learning Outcomes to Program Objectives (1-5)         P1       P2       P3       P4       P5       P6       P7       P8       P9       P10       P11         1       5       5       5       3       4       4       5       4       5         2       5       5       5       3       4       44       5       4       5         3       5       5       5       3       4       4       5       4       5         4       5       5       5       3       4       4       5       4       5         3       5       5       5       5       3       4       4       5       4       5         4       5       5       5       3       4       4       5       4       5         5       5       5       5       3       4       4       5       4       5         4       5       5       5       3       4       4       5       4       5         4       5 <th colspan="5"></th>					
P1         P2         P3         P4         P5         P6         P7         P8         P9         P10         P11           1         5         5         5         5         3         4         4         5         4         5           2         5         5         5         3         4         4         5         4         5           3         5         5         5         3         4         4         5         4         5           3         5         5         5         3         4         4         5         4         5           4         5         5         5         3         4         4         5         4         5           4         5         5         5         3         4         4         5         4         5           4         5         5         5         3         4         4         5         4         5           5         5         5         3         4         4         5         4         5           5         5         5         3         4         4					
P1         P2         P3         P4         P5         P6         P7         P8         P9         P10         P11           1         5         5         5         5         3         4         4         5         4         5           2         5         5         5         5         3         4         4         5         4         5           3         5         5         5         5         3         4         4         5         4         5           3         5         5         5         5         3         4         4         5         4         5           4         5         5         5         5         3         4         4         5         4         5           4         5         5         5         5         3         4         4         5         4         5           4         5         5         5         3         4         4         5         4         5           5         5         5         3         4         4         5         4         5           5					
1       5       5       5       5       3       4       4       5       4       5         2       5       5       5       5       3       4       4       5       4       5         3       5       5       5       5       3       4       4       5       4       5         3       5       5       5       3       4       4       5       4       5         4       5       5       5       3       4       4       5       4       5         4       5       5       5       3       4       4       5       4       5         4       5       5       5       3       4       4       5       4       5         4       5       5       5       3       4       4       5       4       5         5       5       5       5       3       4       4       5       4       5         5       5       5       5       3       4       4       5       4       5         6       5       5       5       3					
2       5       5       5       5       5       3       4       4       5       4       5         3       5       5       5       5       5       3       4       4       5       4       5         4       5       5       5       5       3       4       4       5       4       5         4       5       5       5       5       3       4       4       5       4       5         4       5       5       5       5       3       4       4       5       4       5         5       5       5       5       5       3       4       4       5       4       5         5       5       5       5       3       4       4       5       4       5         5       5       5       5       3       4       4       5       4       5         6       5       5       5       5       3       4       4       5       4       5	P12				
3       5       5       5       3       4       4       5       4       5         4       5       5       5       5       3       4       4       5       4       5         4       5       5       5       5       3       4       4       5       4       5         5       5       5       5       3       4       4       5       4       5         5       5       5       5       3       4       4       5       4       5					
4       5       5       5       5       3       4       4       5       4       5         5       5       5       5       5       5       3       4       4       5       4       5         5       5       5       5       5       5       3       4       4       5       4       5					
<b>5</b> 5 5 5 5 5 3 4 4 5 5					
<b>6</b> 5 5 5 5 5 3 4 5 5 5 5 3 <b>6</b> 5 <b>6</b> 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5					
<b>7</b> 5 5 5 5 5 3 4 5 5 5					
<b>8</b> 5 5 5 5 5 3 4 5 5 5 3 <b>6</b> 5 5 5 <b>8</b> 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5					
<b>9</b> 5 5 5 5 5 3 4 5 5 5					
<b>10</b> 5 5 5 5 5 3 4 5 5 5					
<b>11</b> 5 5 5 5 5 3 4 5 5 5					
<b>12</b> 5 5 5 5 5 3 4 5 5 5					
<b>13</b> 5 5 5 5 5 3 4 5 5 5					
14         5         5         5         5         3         4         4         5         4         5					
Contribution Level         1: Low 2: Low-intermediate 3: Intermediate 4: High 5: Very High					
https://obs.tau.edu.tr/oibs/bologna/progLearnOutcomes.aspx?lang=en&curSunit=196					
Compiled by: DI Dr. Canan Yıldız					
Date of Compilation: 16.03.2020					